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KINEMATICS OF MACHINES

AN ELEMENTARY TEXT-BOOK

BY

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PREFACE.

THIS book is intended as a brief manual for Engineering Students, and treats chiefly of those portions of the subject of the Kinematics of Machines which are likely to be of assistance in the study of the Dynamics of Machines and in work in Machine Design.

The author wishes to thank his friends and colleagues, Dr. E. G. Coker and Mr. H. M. Jaquays, for their kindly criticism and for their help in revision of the proof-sheets.

Many earlier works have been consulted in the preparation of this volume ; wherever possible they are named in the text or in foot-notes. Professors John H. Barr and C. W. MacCord have courteously permitted the use of certain of their diagrams, and the author is indebted to The American Stoker Company, The Brown and Sharpe Manufacturing Company, and The Link Belt Engineering Company for the use of figures and information.

MONTREAL, November 1902.

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