# The ADR rule-of-thumb as predictor of lodging property values

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In a positive context, asset valuation models may be judged on the basis of their predictive ability rather than on the number and elegance of the underlying assumptions. The Average Daily Rate (ADR) rule-of-thumb has been used for decades as a quick way of estimating hotel and motel room rates and, more recently, as a simple gross-income multiplier model for predicting values of lodging properties. This study examines how well the ADR rule-of-thumb model predicts property values. The results of our comparative analysis of estimates from the ADR model with those from a hedonic valuation model indicate that the ADR model performs well in the aggregate, but is an inconsistent estimator at various levels of disaggregation, such as when property subsamples were organized by number of rooms, age, occupancy rate and number of restaurants.

Key words: ADR rule-of-thumb valuation models lodging properties

#### Introduction

In his classic Essays in Positive Economics, Milton Friedman characterized economics as a positive science consisting of generalization about economic phenomena that may be used for prediction (Friedman, 1935). Theories in 'positive' economics are not judged on the basis of the realism or elegance of their assumptions, but rather, on their ability to predict the outcomes from human interactions. Neoclassical economics has produced an assortment of models for valuing real estate. Some of these models are quite simplistic in their underlying assumptions, while others have many detailed assumptions. The trend in real estate valuation has been toward development and application of models with explicit and detailed sets of assumptions. Less structured models may be useful (in a positive context) for valuation only if empirical tests show that they have predictive power.

Application of simple ratio models based on the relationship between either the development or reproduction cost and average daily room rate (ADR) of hotels and motels has a longstanding tradition in the lodging industry. The development costs of properties have been used as the economic foundation for deriving quick estimates of how much to charge per night for rooms (Vallen and Vallen, 1991; Kasavana and Brooks, 1991). Sometimes observed room rates are used to easily generate estimates of the values of properties. When used for valuation purposes, the relationships take the following forms:

$$V = ADR (1000) (R)$$
 (1a)

and

$$V/R = ADR (1000),$$
 (1b)

where V is the value of the lodging property, ADR is the average daily rate from lodging property operations, and R is the number of available rooms.

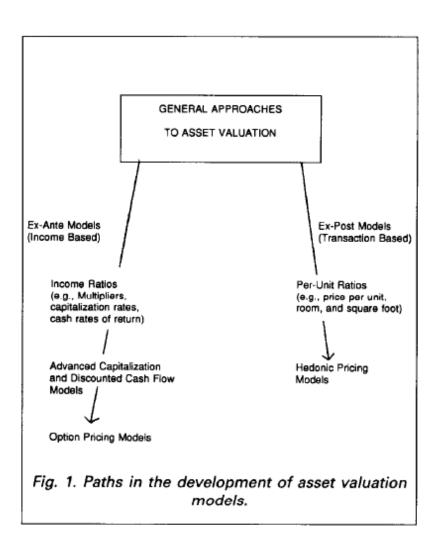
In this paper, we compare value estimates from the ADR rule-of-thumb model to value estimates from an economic fundamentals model. The economic fundamentals model is a hedonic pricing model that has been customized for lodging property valuation. In the aggregate, the ADR rule-of-thumb model yields estimates of lodging property values that only differ slightly from hedonic estimates. When the property sample is disaggregated, using physical characteristics and financial performance characteristics as the cross-¬sections, many statistically significant differences in the estimates from the two models are found. These results suggest that care must be taken when interpreting results from aggregate comparative analyses of the hotel and motel values.

The balance of the paper is organized into three sections. The next section presents the background of rule-of-thumb valuation models and specifically the ADR rule. The section that follows describes the development of the economic fundamentals model and how the comparative analysis was performed. The findings and conclusions from the study are contained in the final section.

### Rule-of-thumb models in perspective

The modern convention in asset valuation is for models to be heavily structured with assumptions and for rigorous statistical estimation of model parameters. Figure 1 traces two historical paths in the development of asset valuation models. The ex-ante models shown along one path are based on the concept that buyers and sellers make decisions from forecasts of future incomes. The simple, rule-of-thumb models found along the early part of this path rely on few assumptions about future incomes. Discounted cash flow and option pricing models attempt to capture the economic fundamentals of decisions through precision in the estimation of future incomes and through explicit recognition of market participant behavior.

Ex-post models, shown along the second path, are conceptually based on the idea that buyers and sellers make decisions from knowledge of recent transactions in the space and asset markets. Rule-of-thumb models of this variety relate prices to the physical characteristics of assets. And as with income-based rule-of-thumb models, much judgment is required to reach value conclusions. By contrast, hedonic models introduce a broader spectrum of physical and other asset characteristics and bring greater objectivity to transaction-based valuation.



#### Previous literature

Advances in modelling asset value may be critically examined by subjecting the models to the rule of parsimony. During the 1950s and 1960s, studies by Gordon (1955) and Sarnat and Levy (1969) concluded that the reciprocal of the payback period, a rule-of-thumb model, and the internal rate of return, a fundamentals model, produce different results that are predictable in a limited set of cases. These studies, which were limited to investments with level incomes and zero residual values, found accounting return to be an inaccurate measure of internal rate of return and the errors between accounting return and internal rate of return are neither constant nor consistent (see Livingston and Solomon, 1970 for a review of the early studies). Recently, Fama and French (1992) presented surprising evidence that simple size ratios and equity ratios explain cross-sectional stock returns better than the Capital Asset Pricing Model.

From the literature comparing real estate valuation models, Smith (1985) describes the limiting conditions under which traditional rule-of-thumb models such as gross-income multipliers, overall capitalization rates, and cash-on-cash measures of real estate return will approximate discounted cash flow (DCF) model results for multi-family properties. These limiting conditions, however, are sufficiently restrictive to make it improbable that rule-of-thumb and DCF models will yield consistent results. Lusht (1978) found no meaningful relationships between rule-of-thumb models, particularly first-year cash flow and DCF results. Geltner et al. (1991), who compare real estate capitalization rates derived from a simple mortgage-equity formula with those from an economic fundamentals model, also find no relationships. Mitchell and Bernes (1992), however, report strong correlations when comparing value estimates for multi-family properties using income and physical/transactional ratios (e.g. rent per square foot) versus hedonic model estimates.

Intuitively, models that are driven by assumptions closely resembling economic fundamentals for which the parameters are estimated objectively, should produce different estimates than rule-of-thumb models. The literature provides general verification of this notion, yet there may be circumstances under which the differences are either small or predictable.

The literature on lodging property valuation is not highly developed relative to advancements in modelling values of other capital assets. Further, there are no published studies that compare estimates of lodging property values from alternative valuation models. The comparative analysis of a simple rule-of-thumb model and a sophisticated sales comparison model performed in this study thus begins to fill the large void in our understanding of how to value perhaps the most important assets on the balance sheets of lodging and related companies.

### The ADR rule-of-thumb

As in other industries, rules-of-thumb are part of the heritage of the lodging industry. An often expressed industry standard, for example, is that the number of employees needed in a full service lodging operation is equal to the number of available rooms. \* Room rates are equated to property development costs and values in similar ways by traditional standard. The rule that \$1 of ADR equals \$1000 of development costs is evidenced through examples found in several early hotel management (Podd and Lesure, 1964) and marketing (Coffman, 1970) texts. In their 1991 text, Vallen and Vallen refer to the rule as the 'building cost method' for evaluating room rates. Use of the rule is characterized as analogous to an old cookbook direction—'flavor to taste'. Yet, they note that the rule is still applied directly on the theory that rising construction costs are matched by rising room rates. Advocates of the rule also may argue that it works more effectively for economy hotels. Kasavana and Brooks (1991), in another recent hotel management text, recom—mend that the rule be restructured as a relationship between ADR and the replacement cost of the hotel to adjust for inflation.

<sup>\*</sup> Most of the limiting conditions require constant relationship for incomes and expenses across properties and over time. See smith (1985, pp. 548-550)

Rushmore's (1990a, 1990b) writings legitimize the ADR rule-of-thumb as an alternative model for valuing new and existing lodging properties. Yet, he makes it clear that the reliability of the model for general usage is questionable. In Rushmore (1990b), an existing property's value is estimated consistently with the room rate multiplier and six other valuation models. (Room rate multiplier is ADR x  $1000 \times R$ .) In Rushmore (1990a), the rule is presented along with cautionary notes. Implicit in the rule are assumptions about occupancy, ratio of food and beverage revenue to rooms revenue, and other costs and expenses. The multiplier, therefore, should be adjusted if the subject property's operating characteristics vary from those assumed for direct use of the rule. This model should be used to 'establish broad parameters for room rates and project value' (pp. 11-17).

The advantages of applying the ADR rule-of-thumb model for valuation are clearer than the disadvantages. In exchange for ease and expedition, many assumptions must be made implicitly, and a high degree of subjectivity is introduced to reach value conclusions from the ADR model.

### Relationships between ADR rule and capitalization rate

As with any gross-income multiplier, and ADR multiplier, 1000(R), may be converted to an annual capitalization rate by making some explicit market and property assumptions. Let ARR be annual room revenues so that:

$$ARR = ADR 365(R) \tag{2}$$

and

$$ADR = ARR/365(R). (3)$$

Substituting equation (3) into the ADR rule-of-thumb equation (1a):

$$V = ADR (1000)(R)$$

gives an annual gross income multiplier model:

$$V = 2.7397 \text{ (ARR)}.$$
 (4)

If average annual occupancy is assumed to be 70%, the annual operating expense ratio is 60% and there is no food and beverage revenue then the net operating income (NOI) multiplier is

$$V = 9.78$$
 (NOI),

and the capitalization rate is 10.22%.

### Testing and the ADR rule

To determine whether the ADR rule-of-thumb model is a reliable, as well as quick and easy valuation tool, we compare the value estimates from the ADR model to value estimates from a model based on the fundamental economic characteristics of properties. This section describes the property sales data and how the fundamentals model is developed.

# **Property sales**

A data base contains over 1,100 lodging property sales occurring from 1985 and 1991. In addition to the observed sale price, over 100 pieces of information are recorded for each sale, including details about the property's

physical characteristics, ownership form, location, and local market conditions. Table 1 presents selected information available for most transactions (see Corgel and deRoos, 1992) for a more complete description of these data).

Over one-half of the sales in the data base have been omitted from consideration in this

Variable name	Description		
S	Selling price adjusted for extraordinary financing and ground leases		
R	Either ADR or published single occupancy rate at time of sale (ADR used in regressions)		
OCC	Occupancy at time of sale		
ROOM	Number of rooms at time of sale		
AGE	Age in years at time of sale		
MEET	Properties with meeting and banquet facilities		
BUY,SEL	Ownership form of buyers and sellers including individuals, partnerships, domestic real estate corporation, domestic hotel corporation, foreign corporation, domestic institution, and foreign institution		
CHAN	Affiliation with major lodging chain		
LTD	Limited service lodging facility		
DELX	Properties with high levels of amenities		
SUIT	All suite lodging properties		
GOLF	Properties with golf as an amenity		
TEN	Properties with tennis as an amenity		
POOL1-N	Properties with one or more pools		
REST1-N	Properties with one or more food and beverage operations		
AIR	Properties within two miles of an airport		
тсом	Time in minutes between a property and the nearest commercial center		
EMP	Number of employed persons in the county during the month of sale		
EMPC	Change in EMP (annual rate)		
EBI	Effective buying income per capita in the county during the year of sal		
Y85_Y91	Year of sale		

study because either the published room rate is available instead of the ADR, occupancy is unavailable, or the property has extraordinary characteristics, such as casino gaming. The final sample of 513 sales has the general statistical profile shown in Table 2. None of these properties was taken out of service following the sale.

### Fundamentals model

The common practice in studies of this type is to compare the rule-of-thumb model estimates to those of a fundamentals model. The fundamentals model may be either income-based (Gordon, 1955; Sarnat and Levy, 1969; Lusht, 1978; Geltner etal., 1991) or transaction-based (Mitchell and Bernes, 1992). We use a two-equation, transaction-based model to obtain estimates of the market value of lodging properties. The equations for room rate and for sale price have the following functional forms:

$$R_i = r(O_i, M_i, P_i, L_i, E_i, T_i; \beta, e)$$
(5)

$$S_i = s(P_i, L_i, E_i, C_i, Q_i, T_i; \beta^*, u), \qquad (6)$$

where

Variable	Number of observations	Mean	Standard deviation
Sale price (adjusted for financing)	513	\$9,362,922	\$20,700,818
Average daily rate	513	\$49.06	\$28.64
Number of rooms	513	164	112
Average occupancy	513	61.39%	12.48%
Age	513	14 years	15 years
Number of restaurants		-	-
Zero	186		
One	249		
Two	61		
Three	14		
Four	3		
Year of sale			
1985	44		
1986	63		
1987	42		
1988	104		
1989	128		
1990	116		
1991	16		

$R_i$	is the room rate of the ith property at time of sale
$S_i$	is the cash equivalent sale price of the ith property
$O_i$	is the occupancy of the ith property at time of sale
$M_i$	is the market segment of the ith property at time of sale
$P_i$	is a vector of property characteristics of the ith property at the time of sale
$L_i$	is a vector of locational characteristics of the ith property at the time of sale
$E_i$	is a vector of economic characteristics of the local area in which the ith
	property is located at time of sale
$C_i$	is a vector of sale contract characteristics of the ith property transaction
$T_i$	is the year of sale of the ith property
$Q_i$	is an unobserved quality measure of the ith property at the time of sale
$\beta$ , $e$ , $\beta$ *, $u$	are estimated parameters of the models and error terms.

A two-step estimation procedure is used to measure the effect of omitted quality variables. First, the room rate equation is estimated in a semi-log, OLS regression with occupancy, market segment, property characteristics, locational

characteristics, local area characteristics, and time (year) dummies on the right side. Then, the residual from this regression (Q) is introduced as an explanatory variable in the sale price equation. The sale price equation has cashequivalent sale price on the left side, and on the right side, the same property, location, and local market variables as the rate equation plus information about the buyers and sellers in the transactions. The buyer and seller categorical variables are entered in the price equation to pick up unique motivational considerations and informational problems associated with the parties in the contracts for sale. For example, certain investor types may have overpaid for properties as the result of tax transfer opportunities (e.g. limited partnerships) and poor market information (e.g. foreign investors). Similarly, the room rate equation contains variables not found in the price equation. Occupancy is included to account for demand and supply interactive effects as are the market segment variables (i.e. suite, limited service, deluxe, and middle market).

Experiments with various functional forms revealed that the semi-log form provided the best fit of the data. The variances of the equations are adjusted using a heterostedasticity consistent covariance matrix following White (1980) and the severity of collinearity among the explanatory variables is low to moderate.

The estimated room rate equation is (t-statistics are calculated using heterostedasticity consistent standard errors):

N = 513,  $R^2ADJ = 0.5946$ , SEE = 0.2753, Mean LOG(R) = 2.785

The estimated sale price equation is (t-statistics are from heterostedasticity consistent standard errors):

<sup>\*</sup>Significant at 0.05 level.

<sup>†</sup>Significant at 0.01 level.

$+0.2425 \; BUYP$	$+0.1874\ BUYDC$	+0.3464 BUYDI	+0.4429 BUYF
(3.57)†	(3.01)†	(3.38)†	(3.67)†
+0.1677  SELP	+0.1046 SELDC	−0.2107 SELDI	-0.0763  SELF
(2.33)*	(1.54)	(2.93)†	(0.36)
+0.0178 Q	+0.0446 Y86	−0.1617 <i>Y87</i>	-0.0928 Y88
(14.92)†	(0.55)	(1.62)	(3.48)†
-0.2930 Y89	-0.3277 Y90	-0.3653 Y91	
(3.47)†	(3.67)†	(2.67)†	

N = 513,  $R^2ADJ = 0.8466$ , SEE = 0.4593. Mean LOG(CEP) = 15.2056.

The purpose of estimating these equations is not to test specific hypotheses, but instead to generate estimates of value from a fundamentals model. Yet, some interesting observations about the parameters are offered. First, property characteristics such as the number of rooms, age, pools, meeting rooms, and food and beverage facilities have statistically significant relationships to room rates and sale prices. Second, several of the buyer and seller categorical variables, which attempt to capture the incentives of different types of market participants, are important. Third, the location variables AIR and TCOM are surprisingly unimportant in these equations. Finally, the local and economic variables have a large and statistically significant effect on room rates and sales prices.

# Findings from the comparative analysis

Both the ADR rule-of-thumb model and the fundamentals model yield a value prediction for each property in the sample. The sample means of \$9,705,850 (rule-of-thumb) and \$9,578,474 (fundamentals) are only \$127,376 apart. The rule-of-thumb model overpredicts by a mere 1.3% and the difference between predictions is not statistically different from zero. In addition, the standard deviation of the rule-of-thumb prediction is one half of the fundamentals model prediction.

When the sample is disaggregated by key property and operating characteristics, the comparative analysis produces results that are quite different from the results using the entire sample. Table 3 presents the mean differences (DIF) between predictions from the rule-of-thumb model and the fundamentals model for selected property and operating characteristics. In addition to mean values and standard errors, the f-tests are reported for various levels of each characteristic. A t-statistic that is significant either at the 0.01 or 0.05 level is indicative that the two models produce significantly different market value predictions. In such cases, the rule-of-thumb equation is not considered to be a reliable valuation model.

# Univariate analysis

The series of univariate t-tests is performed on variables that, in theory, reveal whether the rule-of-thumb model overpredicts or underpredicts lodging property value. Two physical property characteristics are tested; the number of rooms (ROOM) and the age of the property {AGE). The variable ROOM is divided into four categories ranging from fewer than 75 rooms to over 300 rooms. Because the number of rooms is a scaler in the ADR rule-of-thumb model, the model may become less reliable as the size of the properties increases. As shown in Table 3, the rule-of-thumb model is reliable for properties with 75–149 rooms, but unreliable for properties in other size categories.

<sup>\*</sup>Significant at 0.05 level.

<sup>†</sup>Significant at 0.01 level.

		Mean difference	Standard	
Variable	N	(rule – fundamentals)	error	t-statisti
Room No.		\$	\$	
<75	97	299,848	59,093	5.07†
75–149	204	1,038,467	610,212	1.70
150-299	154	3,110,381	540,562	5.75t
>300	58	-11,285,994	5,601,949	2.01*
AGE (Yr)		\$	\$	
1	30	-8,858,902	8,516,191	1.04
25	142	88,272	691,985	0.027
6–10	84	2,754,674	518,999	5.31†
11–20	155	1,275,100	1,038,927	1.22
21–50	83	1,758,882	430,509	4.08†
>50	19	-14,244,435	8,759,776	1.62
R (\$)		\$	\$	
<30	76	682,497	85,375	7.99†
\$30-\$44.99	215	1,512,004	132,691	11.39†
\$45-\$59.99	103	2,541,267	259,019	9.81†
\$60-\$84.99	88	3,164,223	974,615	3.24†
>\$85	31	-27,477,717	10,415,278	2.63†
OCC (%)		\$	\$	
>80	39	567,732	1,796,079	0.31
70-79.99	101	-1,810,239	1,920,571	0.94
60-69.99	167	-668,161	1,642,596	0.40
50-59.99	130	1,363,616	998,750	1.36
<50	76	2,109,859	333,249	6.33†
REST No.		\$	\$	
0	186	966,827	85,200	11.35†
1	249	1,518,099	1,067,471	1.42
2	61	-1,502,168	2,923,501	0.51
3	14	-16,385,373	10,028,844	1.63
1	3	-57,155,095	9,535,184	5.99†
MEET		\$	\$	
<b>Vith</b>	370	-227,561	992,359	0.22
Vithout	143	1,045,746	166,805	6.27†
Y		\$	\$	
1985	44	-99,695	\$ 862,291	0.12
1986	63	-5,322,587	2,998,555	1.77
1987	42	2,092,092	324,347	6.45†
988	104	529,693	959,240	0.55
1989	128	1,676,057	1,040,411	1.61
1990	116	211,467	2,239,504	0.09
1991	16	1,439,488	2,684,785	0.53

The rule-of-thumb model traditionally has been used as an aid in decision-making for development of new lodging properties, and to a lesser extent associated with room rates and values of older existing properties. Thus, the ADR model may be more reliable for newer properties than for older properties. The univariate tests, however, suggest no clear relationship between AGE and the reliability of the ADR model.

Because of the implicit assumptions in the ADR model regarding property financial performance (Rushmore, 1990a), the model may predict better at some levels of average room rate (R), occupancy (OCC), restaurant operation

{REST), and business meeting operations {MEET) than others. As in the case of ROOM, R is a scaler in the ADR rule- of-thumb equation. Thus, the ADR model is expected to be less reliable as R increases. The univariate results in Table 3 suggest that the ADR model is unreliable at all levels of R. The model significantly overpredicts value at lower room rates and significantly underpredicts value at room rates greater than \$85.

Because the ADR model only explicitly recognizes room revenue, the model may not be effective in valuing properties with substantial food and beverage and meeting businesses. The univariate f-tests in Table 3 indicate that not only is the model unreliable for valuing properties with four restaurants, but also is unreliable for valuing properties with no food and beverage business. In addition, the ADR model generates predictions that are consistent with the fundamentals model for properties with meeting space, and predictions that are inconsistent for properties without meeting space. These results are contrary to what is expected.

Finally, the univariate comparative analysis is conducted with the year the property sold as the focus variable. During those years that tax advantages from owning real estate had a large role in market behavior, the ADR rule-of-thumb model should be less reliable than for other years. Again, the reasoning for this position is that tax effects are not explicitly recognized in the ADR model. This hypothesis only is supported by the statistics for 1987.

### Multivariate analysis

In addition to the series of univariate tests, a multivariate test is performed using the same list of variables except R which is highly collinear with some other variables. The dependent variable in the regression is the absolute value of the difference between predictions using the ADR rule-of-thumb model and the fundamentals model. The estimated regression equation has the form:

A significant coefficient (positive or negative) suggests that the variable is statistically important for explaining the inefficiency of the ADR rule-of-thumb model, holding other factors constant. The significance of the ROOM variable supports the notion that the ADR rule is less efficient for larger properties. Also, the rule tends to become less efficient as the number of restaurants increases. These results are consistent with our expectations.

#### **Conclusions**

Asset valuation experts will select the simple, parsimonious model over the elaborate, assumption-laden model if the two models perform with equal precision. Given the trend toward the development of stylized valuation models, it is important to confirm that explicit statements of implicit relations indeed constitute advancements in valuation methodology. Our examination of the predictive ability of a simple rule-of-thumb model for valuing lodging properties

<sup>\*</sup>Significant at 0.05 level.

<sup>†</sup>Significant at 0.01 level.

shows that the model is unreliable except in cases in which there are high degrees of data aggregation. Generally, we find that the ADR rule-of- thumb model does not generate predictions that are consistent with an economic fundamentals model, and that the predictions it produces are inconsistent across various types of lodging properties.

Although the ADR model is well understood by professionals, easy and inexpensive to use, and has a longstanding tradition, we conclude that it has limited use as a property valuation tool.

Acknowledgements—The authors wish to extend our sincere appreciation to Stephen Rushmore and Daniel Lesser of Hospitality Valuation Services and the many members of the Hotel Motel Brokers Association for their co-operation in assembling the data for this study. This study could not have been completed without the financial support of the Cornell University School of Hotel Administration.

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