

# Hot Thermodynamics for Freezing Soils

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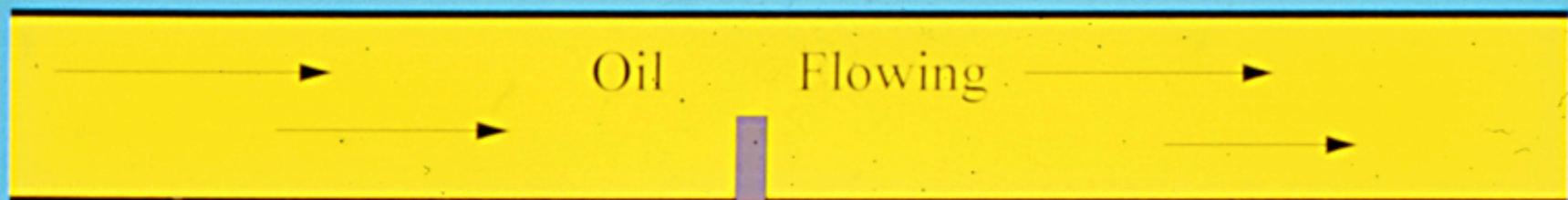
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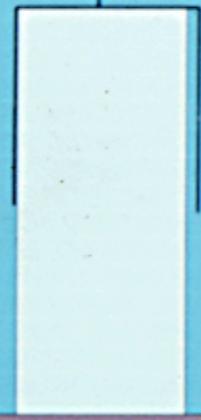
Ontario, CANADA



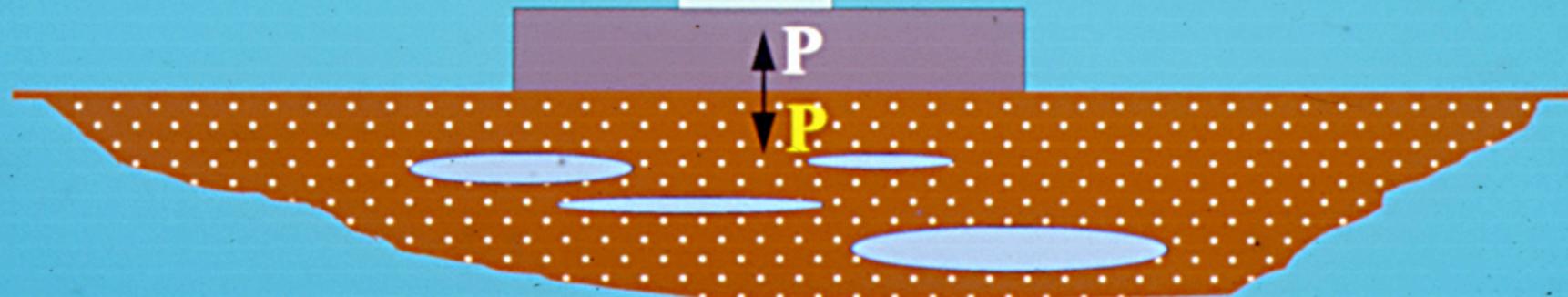




Pipeline



$\uparrow P$   
 $\downarrow P$



# CRREL: Segregation Potential (SP)

$$SP \equiv \nu / (Grad T_{ff})$$

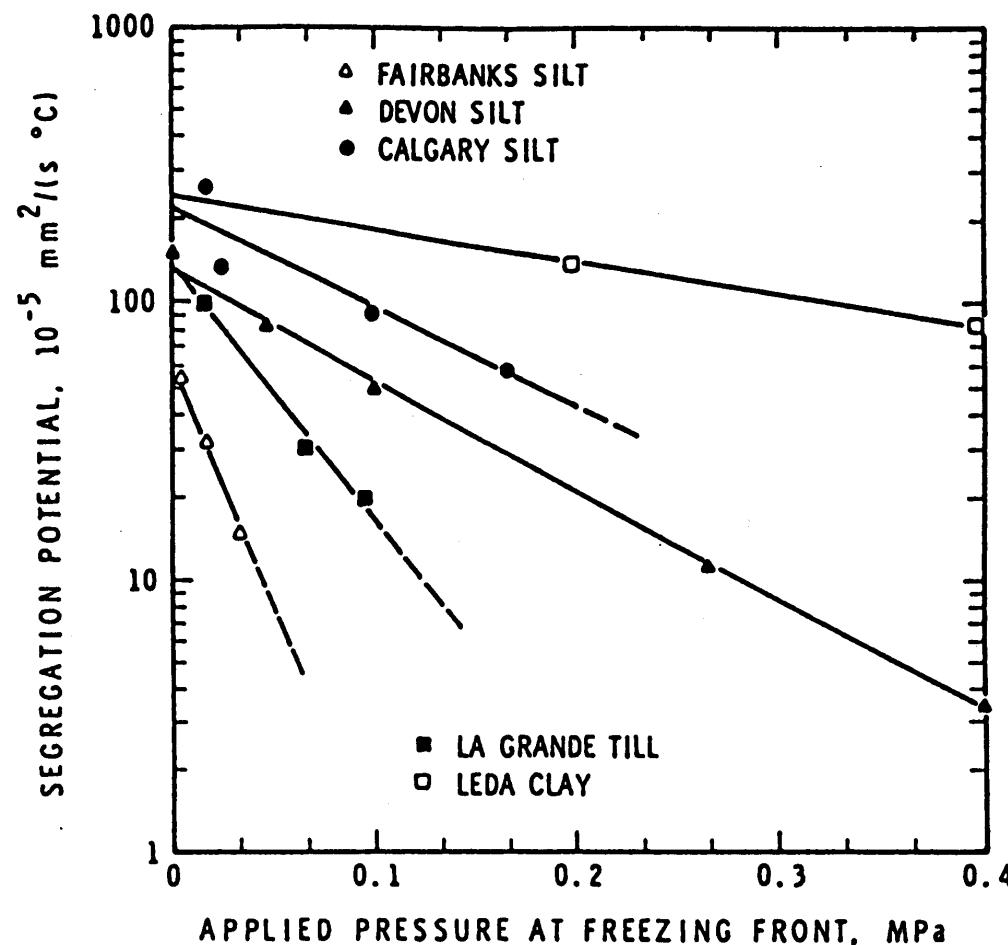


FIGURE 74.4. Summary of data for SP parameter.

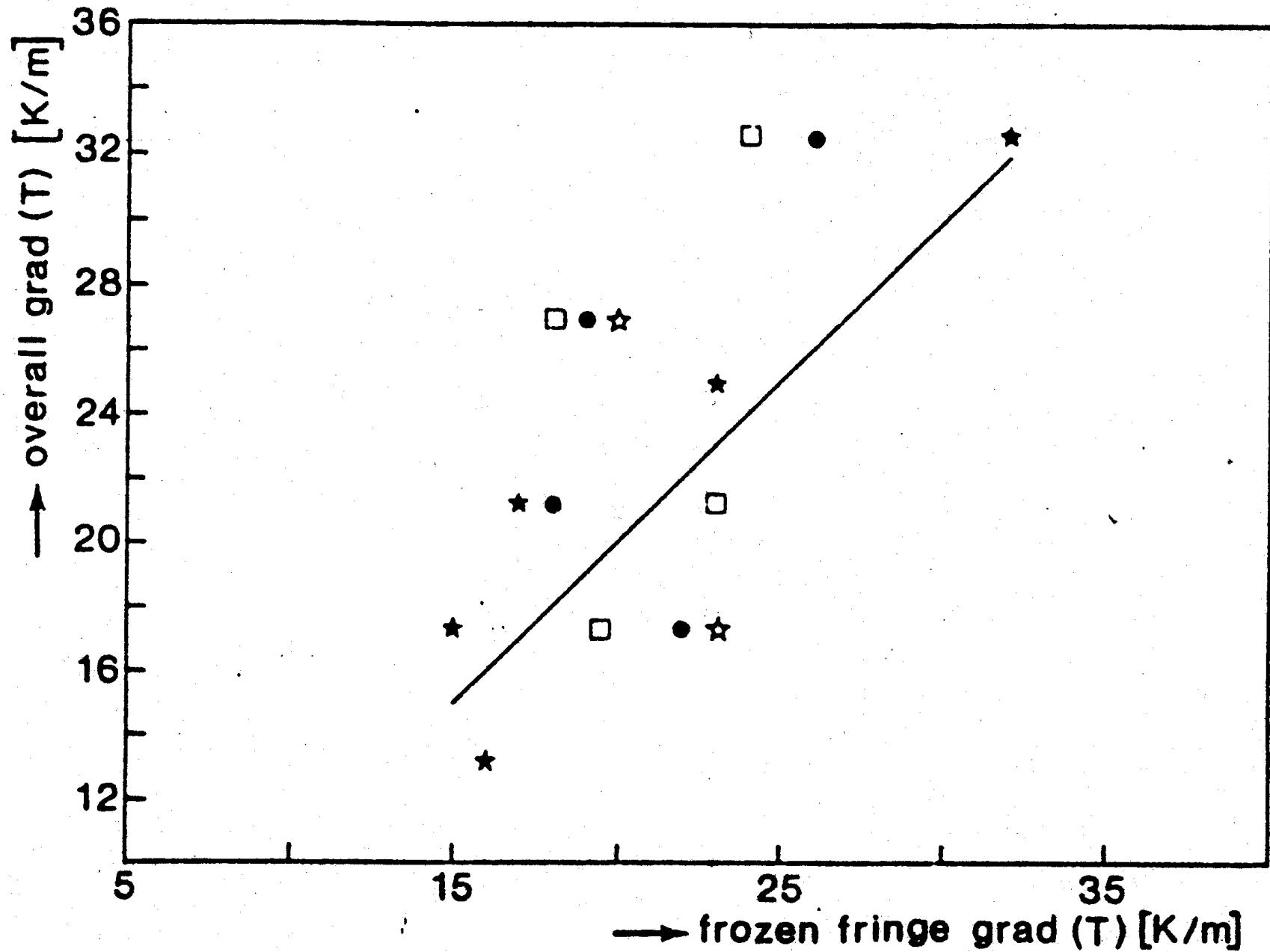
# CORNELL: Heave Rate

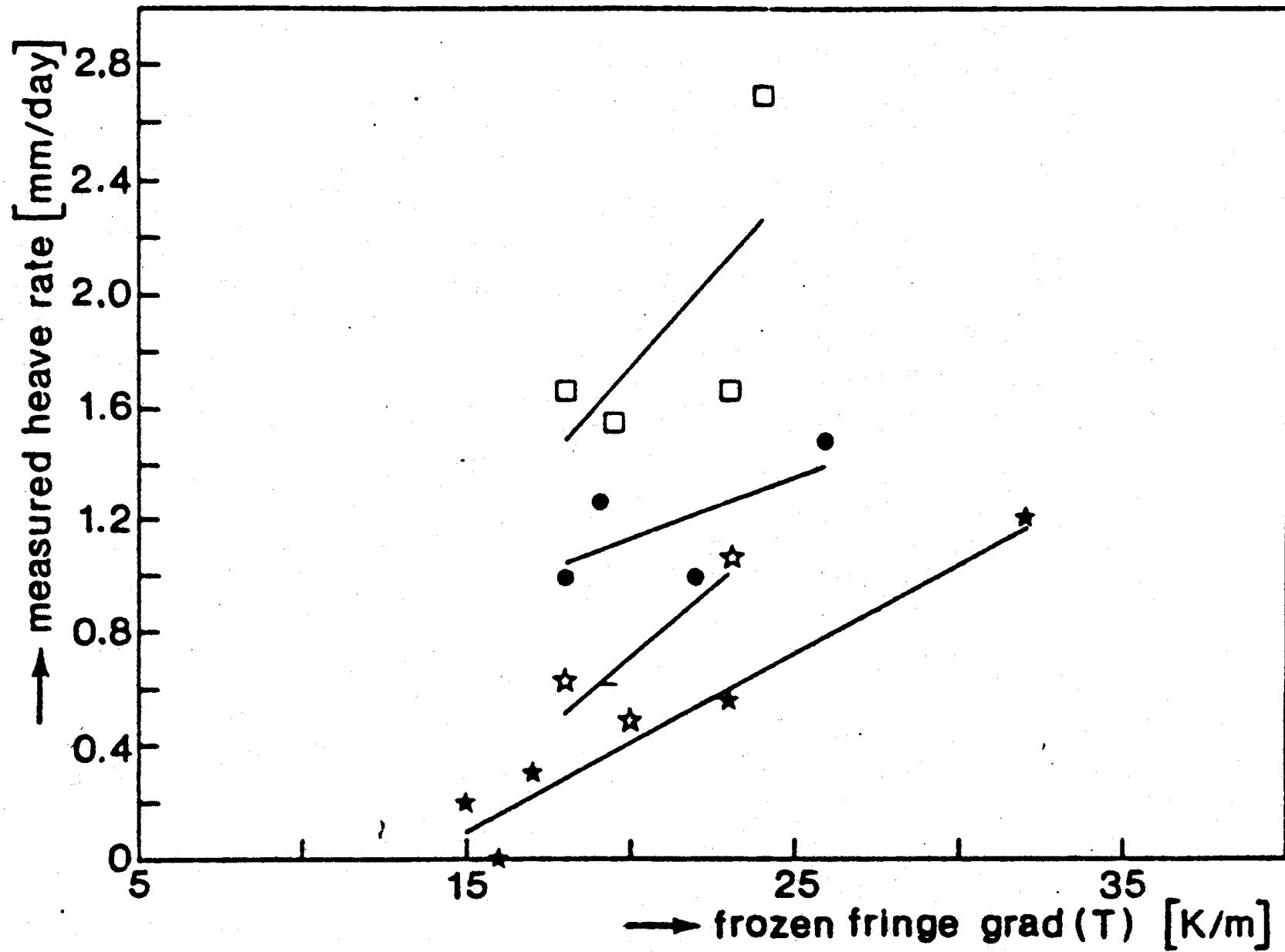
$$dh_{sec}/dt = A - B \times (\partial T / \partial z)_{ff}$$

where  $dh_{sec}/dt$  is the heave rate

and

$$B = SP \times (\rho_w / \rho_i)$$





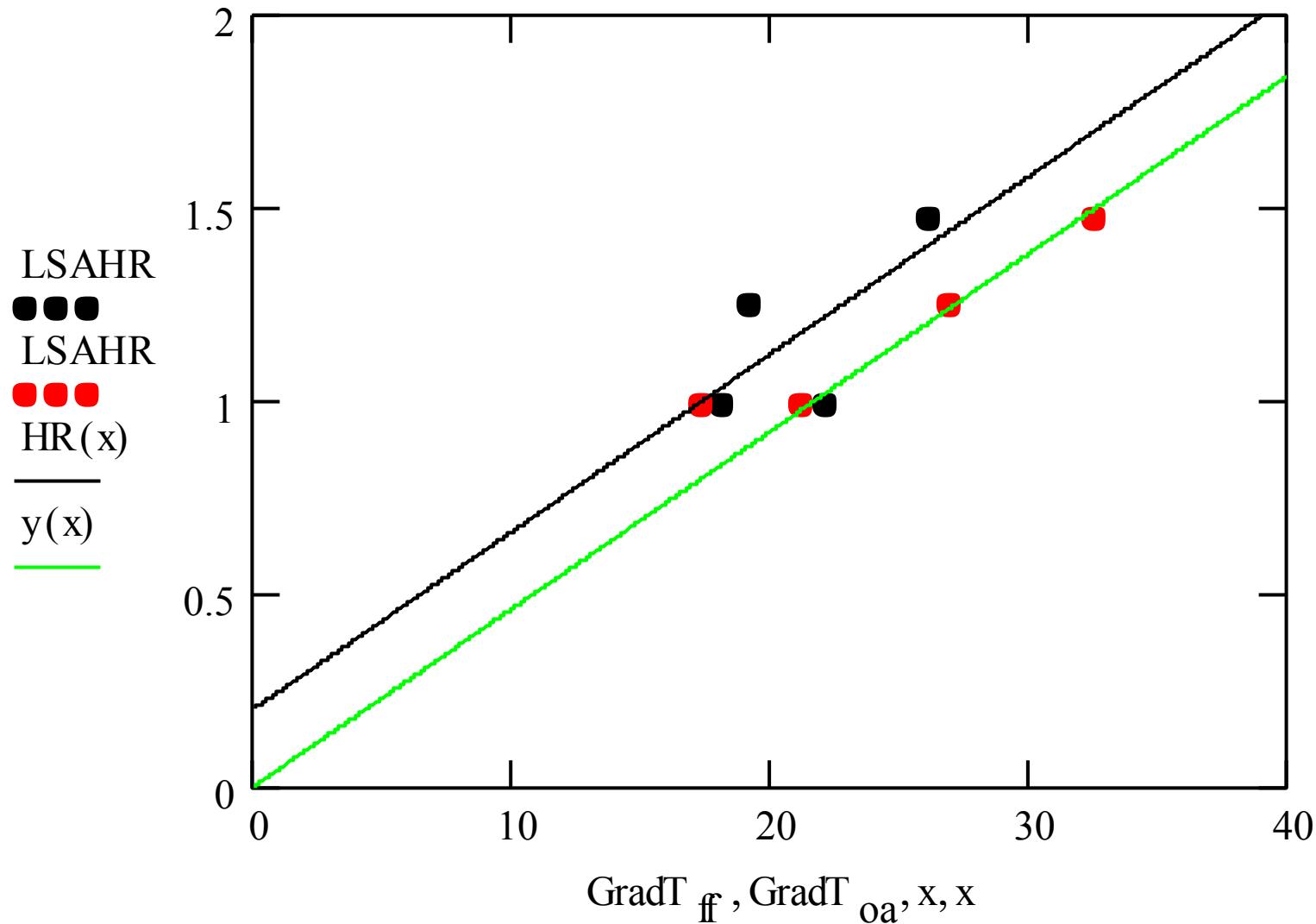
$$A := 0.2$$

$$B := 0.046$$

$$b := 0.046$$

$$HR(x) := A + B \cdot x$$

$$y(x) := b \cdot x$$

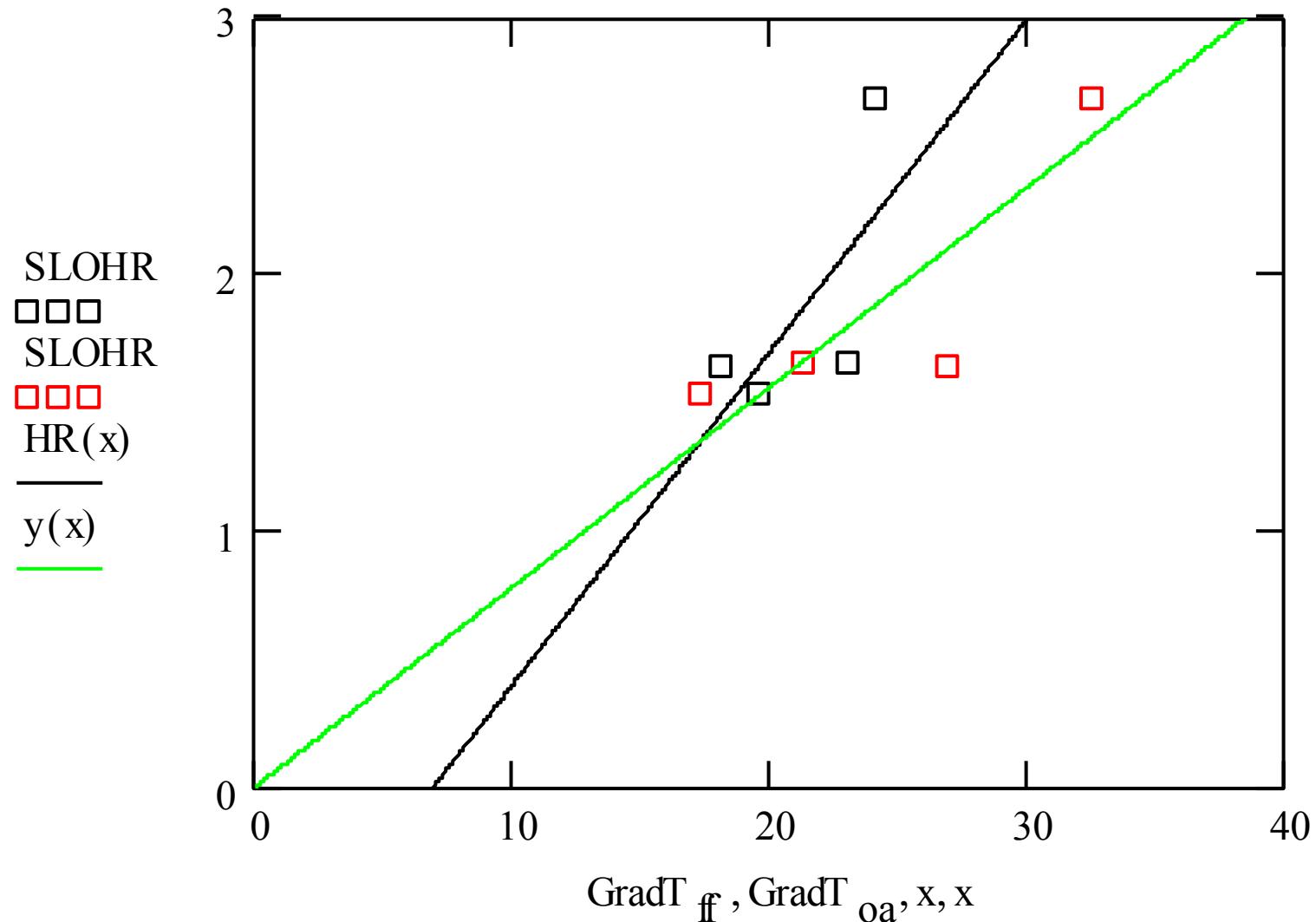


$$A := -0.9 \quad B := 0.13$$

$$b := 0.078$$

$$HR(x) := A + B \cdot x$$

$$y(x) := b \cdot x$$

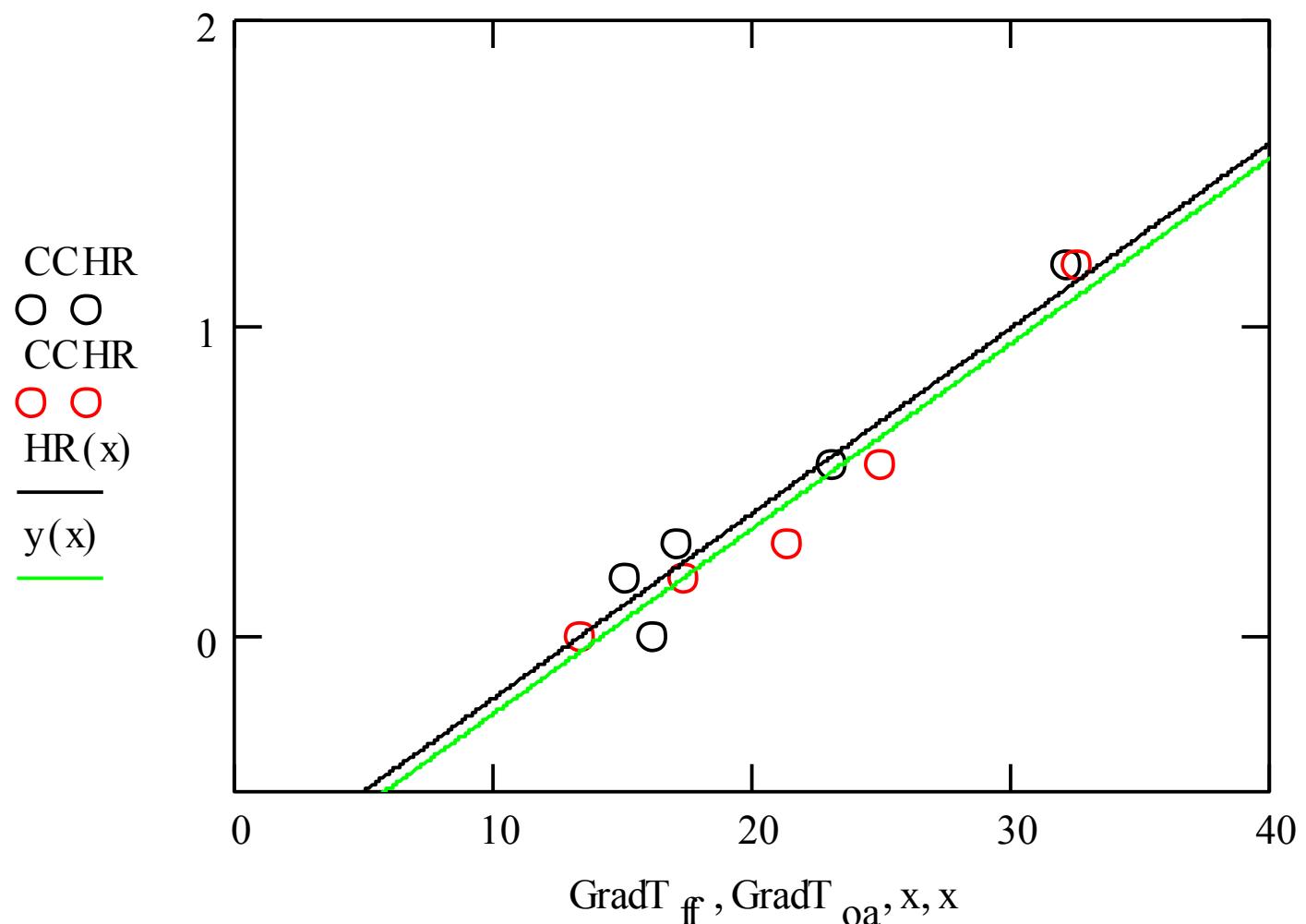


$$A := -0.8 \quad B := 0.06$$

$$a := -0.85 \quad b := 0.06$$

$$HR(x) := A + B \cdot x$$

$$y(x) := b \cdot x + a$$



Clapeyron

$$\bar{V}_i dp_i - \bar{V}_i dp_i = H_f T^{-1} dT$$

$$\bar{V}_i \operatorname{Grad} p - \bar{V}_i \operatorname{Grad} p_i = H_f T^{-1} \operatorname{Grad} T$$

Darcy

$$\nu = -K(\theta_l, \vartheta_i) \operatorname{Grad} p$$

$$HI \equiv v \text{Grad}^{-1}(-T) \quad [m^2 s^{-1} K^{-1}]$$

*Grad(-T) is the overall temperature gradient  
From the soil surface to the frost front*

*(not the temperature gradient in the frozen fringe)*

$$HI = \frac{K}{\bar{V}_l} \left\{ \bar{V}_i \frac{\operatorname{Grad} p_i}{\operatorname{Grad} T} + \frac{H_f}{T} \right\}$$

$$HI = \frac{K}{\bar{V}_l} \left\{ \frac{H_f}{T} \right\} \qquad [m^2\, s^{-1}\, K^{-1}]$$

